

# Origin of the ring ellipticity in the black hole images of M87\*

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## ABSTRACT

We investigate the origin of the elliptical ring structure observed in the images of the supermassive black hole M87\*, aiming to disentangle contributions from gravitational, astrophysical, and imaging effects. Leveraging the enhanced capabilities of the Event Horizon Telescope (EHT)’s 2018 array, including improved  $(u, v)$ -coverage from the Greenland Telescope, we measured the ring’s ellipticity using five independent imaging methods, obtaining a consistent average value of  $\tau = 0.08^{+0.03}_{-0.02}$  with a position angle of  $\xi = 50.1^{+6.2}_{-7.6}$  degrees. To interpret this measurement, we compared it to general relativistic magnetohydrodynamic (GRMHD) simulations spanning a wide range of physical parameters including the thermal or nonthermal electron distribution function, spins, and ion-to-electron temperature ratios in both low- and high-density regions. We find no statistically significant correlation between spin and ellipticity in GRMHD images. Instead, we identify a correlation between ellipticity and the fraction of non-ring emission, particularly in nonthermal models and models with higher jet emission. These results indicate that the ellipticity measured from the M87\* emission structure is consistent with that expected from simulations of turbulent accretion flows around black holes, where it is dominated by astrophysical effects rather than gravitational ones. Future high-resolution imaging, including space very long baseline interferometry and long-term monitoring, will be essential to isolate gravitational signatures from astrophysical effects.

**Key words.** accretion, accretion disks – black hole physics – gravitation – galaxies: active

## 1. Introduction

The Event Horizon Telescope (EHT) collaboration published the first image of a black hole shadow of the supermassive black hole (SMBH) at the center of the giant elliptical galaxy M87, featuring a distinctive ring-like structure (Event Horizon Telescope Collaboration 2019a,b,c,d,e,f). In the context of general relativity (GR), the standard usage of the term “black hole shadow” is defined as the appearance of a black hole illuminated from all directions, including from behind the observer (e.g., Falcke et al. 2000), corresponding to the interior of the so-called critical curve formed by photon trajectories asymptotically approaching bound photon orbits (Gralla et al. 2019). The ring-like structure in EHT images is primarily a “direct image” ( $n = 0$  emission, where  $n$  is the number of half-orbits) that consists of photons from the accretion flow that are strongly lensed by the black hole’s gravity but complete zero half-orbits around it before reaching the observer (e.g., Gralla et al. 2019; Johnson et al. 2020). The “photon ring” is an infinite series of self-similar subrings of light from photons that complete one or more half-orbits ( $n \geq 1$ ) around the black hole before reaching the observer (Johnson et al. 2020). GR predicts that the critical curve is nearly circular for low inclination angles, such as the  $\sim 17^\circ$  inclination estimated for the M87 black hole, M87\* (Mertens et al. 2016). Because the black hole spin introduces asymmetry in the shape of the critical curve, if the EHT can provide observational access to the critical curve then the measurement of its shape is a pathway to spin measurement. In this paper, we use “gravitational ellipticity” to refer to the shape distortion of the critical curve. For M87\*, spin-induced shadow ellipticity is expected to reach up to  $\sim 0.02$  for a spin parameter  $a \sim 0.94$  and inclination  $i = 17^\circ$  (e.g., Fig. 7, Johnson et al. 2020). Moreover, gravitational effects such as the displacement of the inner shadow relative to the photon ring, which are dependent on black hole spin and inclination, can also contribute to observed asymmetries (e.g., Gralla et al. 2019; Chael et al. 2021). Some exotic spacetimes could produce even larger distortions (e.g., Johannsen-Psaltis Metric in Fig. 5 of Younsi et al. 2023).

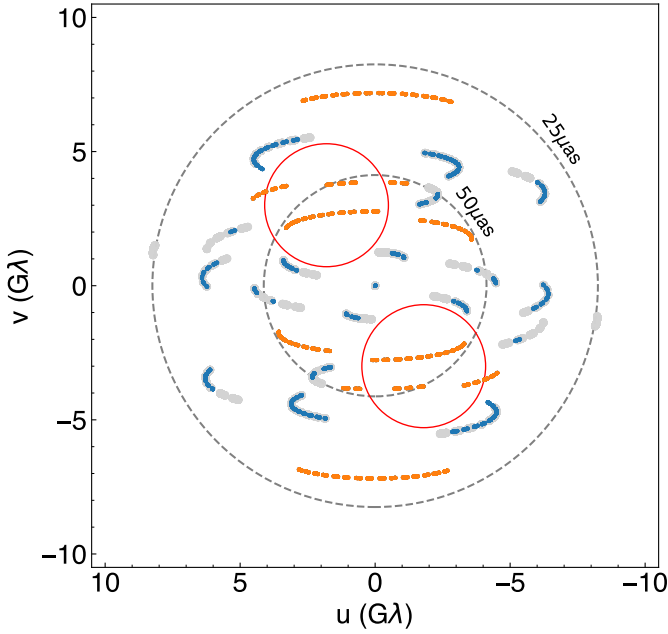
However, very long baseline interferometry (VLBI) observations do not directly resolve the shadow itself, but rather an observed emission structure that appears ring-like due to synchrotron radiation from plasma near the photon orbit (e.g., Event Horizon Telescope Collaboration 2019e, hereafter M87\* 2017 V). This observed shape, which we refer to as the “emission ellipticity”, can deviate from circularity due to asymmetric plasma distributions. For instance, emission from turbulent flows can introduce ring ellipticity (e.g., Tiede et al. 2022a; Tiede & Broderick 2024). Finally, we note that limited  $(u, v)$ -coverage, noise, and algorithmic choices can introduce asymmetries or artifacts in the reconstructed image, even if the

underlying source is circular. In this study, we aim to disentangle the contributions to ellipticity by systematically comparing these two sources: gravitational ellipticity and emission ellipticity. Our goal is to assess the degree to which the observed ellipticity in M87\* EHT images is a result of fundamental spacetime properties, astrophysical factors, or artifacts introduced by imaging algorithms.

In the EHT 2017 results of M87\*, the observed ring-like structure appeared with approximately zero ellipticity, with a diameter of  $42 \pm 3 \mu\text{as}$ . While ellipticity was measured in the reconstructed images ( $\sim 0.05$ – $0.06$ ), no interpretation or calibration was performed (see Figure 18 in Event Horizon Telescope Collaboration 2019f). A subsequent analysis by Tiede et al. (2022a) demonstrated that images reconstructed using the best set of imaging parameter combinations, the so-called Top Set of eht-imaging, could not reliably recover ellipticity, often favoring circular rings and yielding an upper limit of ellipticity of  $\sim 0.3$ . This limitation was primarily due to sparse  $(u, v)$ -coverage, particularly in the north-south direction, as well as the Top Set imaging parameter combinations that were not fully optimized for elliptical models. Later, Tiede & Broderick (2024) reported an M87\* ring ellipticity of  $0.09^{+0.07}_{-0.06}$  using THEMIS, a Bayesian imaging approach that was consistent with general relativistic magnetohydrodynamic (GRMHD) simulations. These results raised important questions about the origins of the ellipticity in the M87\* images and the effectiveness of different imaging methods in accurately recovering it.

The 2018 observations confirmed the persistent structure of the M87\* black hole shadow with a consistent ring diameter of  $43.3^{+1.5}_{-3.1} \mu\text{as}$ , consistent with the 2017 results (Event Horizon Telescope Collaboration 2024, hereafter M87\* 2018 I). However, annual changes in brightness asymmetry were observed with the position angle shifting from about  $180^\circ$  in 2017 to  $210^\circ$  in 2018 which may be attributed to turbulence in the accretion flow. Changes in the brightness asymmetry were previously reported by Wielgus et al. (2020). The addition of the Greenland Telescope (GLT; Inoue et al. 2014) in 2018 substantially improved  $(u, v)$ -coverage (Fig. 1), particularly in the north-south direction, leading to improved image fidelity. We note that the EHT 2018 observations included four frequency bands: two at lower frequencies (band 1 and 2 at 213.1 GHz and 215.1 GHz) and two at higher frequencies (band 3 and 4 at 227.1 GHz and 229.1 GHz). The GLT participated only in bands 3 and 4, so we focused on data from the higher frequency bands in this study. Among the four observing days, we used data from April 21, which had the highest number of participating stations.

In this study, we followed the formalism based on Tiede & Broderick (2024) to measure the ellipticity of the ring-like emission structure in M87\* using the 2018 EHT



**Fig. 1.** EHT 2017 and 2018  $(u, v)$ -coverage. The plot shows observations from April 10, 2017 (gray) and April 21, 2018 (blue and orange). Both are at 229.1 GHz, which corresponds to the hi-band and band 4 in EHT 2017 and 2018, respectively. Orange points highlight the GLT baselines. Red circles show the coverage gaps in 2017, and dashed circles mark the 25 and 50  $\mu\text{as}$  resolution.

observations. We begin by evaluating the precision of ellipticity measurements using a Fisher information analysis in Sect. 2. Next, in Sect. 3, we refine the Top Set imaging parameter combinations for the regularized maximum likelihood (RML) and deconvolution imaging methods from M87\* 2018 I using elliptical crescent models. Additionally, we tested a broader range of elliptical crescent models with various ellipticities and ellipticity position angles to assess any biases in the imaging methods using the data with the new 2018  $(u, v)$ -coverage. In Sect. 4, we apply the same imaging pipelines (and parameter combinations) to the EHT 2018 M87\* data to measure the ellipticity of the M87\* emission ring. We then compare these results with those obtained from GRMHD model reconstructions. Finally, in Sect. 5, we investigate the origin of the observed ellipticity by comparing our results with theoretical models; we provide a summary and conclusions in Sect. 6.

## 2. Fisher information analysis

The Fisher information matrix quantifies the amount of information that observed data carry about certain model parameters  $\theta$ . The Fisher information matrix is given by

$$F_{ij} = \mathbb{E} \left[ \frac{\partial \ln \mathcal{L}(\theta)}{\partial \theta_i} \frac{\partial \ln \mathcal{L}(\theta)}{\partial \theta_j} \right], \quad (1)$$

where  $\mathcal{L}(\theta)$  is the likelihood function of the data conditioned on the parameters  $\theta$ . The terms  $\theta_i$  and  $\theta_j$  are elements of the parameter vector  $\theta$ . The expectation  $\mathbb{E}$  is taken with respect to the probability distribution of the data. For independent Gaussian-distributed data with variance  $\sigma^2$ , the Fisher matrix simplifies to

$$F_{ij} = \sum_k \frac{1}{\sigma_k^2} \left( \frac{\partial V_k}{\partial \theta_i} \frac{\partial V_k^*}{\partial \theta_j} + \frac{\partial V_k^*}{\partial \theta_i} \frac{\partial V_k}{\partial \theta_j} \right), \quad (2)$$

where  $V_k$  represents the observed complex visibilities. The inverse of the Fisher information matrix gives the covariance matrix of the parameter estimates. Hence,  $\Sigma = F^{-1}$ , where  $\Sigma_{ij}$  represents the covariance between parameters  $\theta_i$  and  $\theta_j$ . We assumed a Gaussian posterior distribution for the parameters, where the standard deviations are given by the square root of the diagonal elements of the covariance matrix,

$$\sigma_i = \sqrt{\Sigma_{ii}}, \quad (3)$$

which represents the uncertainty in the estimation of each parameter  $\theta_i$ .

Given the improved EHT array in 2018, as shown in Fig. 1, we estimated the precision with which the EHT can measure ellipticity using Fisher information analysis.

For this analysis, we used an extension of the m-ring model from Johnson et al. (2020). This model has a simple analytic form in both the image and visibility domains, with analytic gradients. This model was also used for the feature extraction done in Event Horizon Telescope Collaboration (2019d, hereafter M87\* 2017 IV) and M87\* 2018 I, making it useful for physical interpretation. The m-ring model consists of a thin ring with nonuniform brightness in azimuthal directions given by a Fourier series. In polar coordinates  $(\rho, \varphi)$ , it is defined as

$$\mathcal{I}(\rho, \varphi) = \frac{S}{\pi d} \delta \left( \rho - \frac{d}{2} \right) \sum_{k=-m}^m \beta_k e^{ik\varphi}, \quad (4)$$

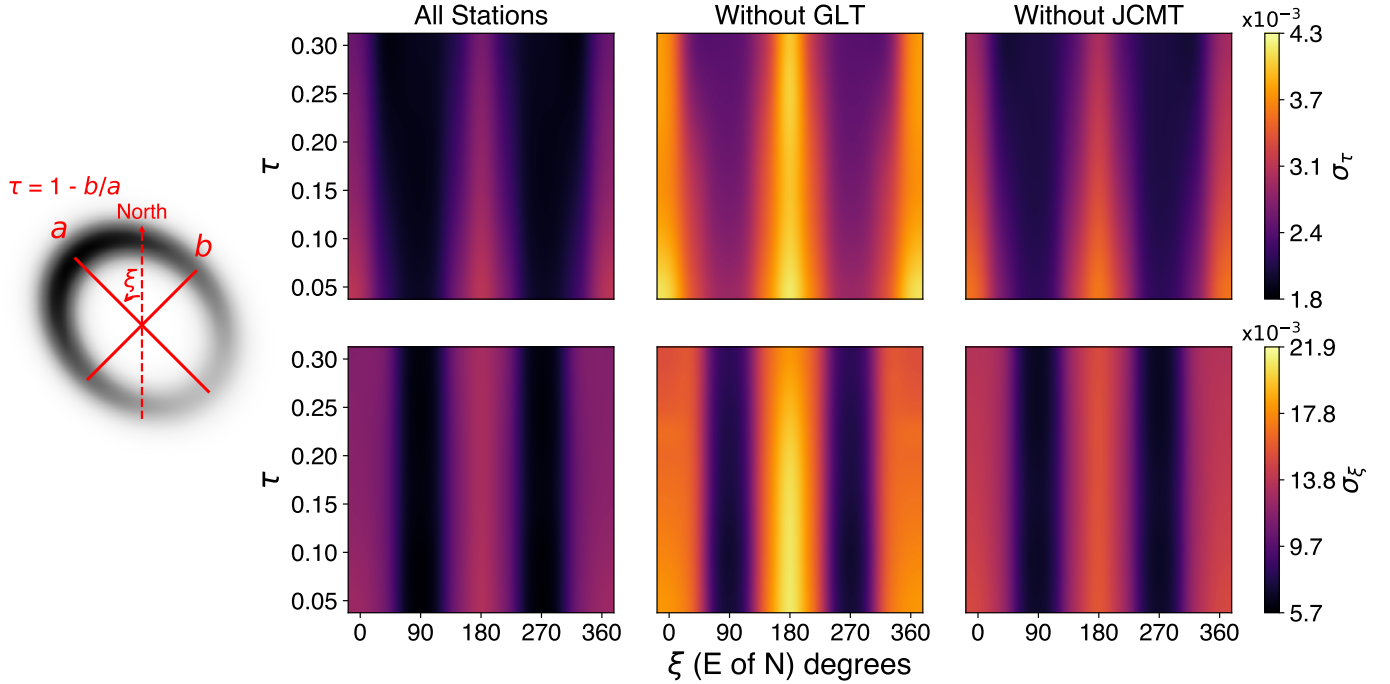
where  $S$  is the total flux density of the ring,  $d$  is the diameter of the ring,  $\delta$  is the Dirac delta function. The coefficients satisfy  $\beta_{-k} = \beta_k^*$  for a real image, and we set  $\beta_0 = 1$  to ensure that  $S > 0$ . The parameter  $m$  represents the azimuthal order of the m-ring. A finite-width m-ring is obtained by convolving Eq. (4) with a Gaussian of FWHM  $\alpha$ . This blurred m-ring is given by

$$\begin{aligned} \mathcal{I}(\rho, \varphi; \alpha) &= \frac{4 \ln 2}{\pi \alpha^2} S \exp \left( -\frac{4 \ln 2}{\alpha^2} (\rho^2 + d^2/4) \right) \\ &\times \sum_{k=-m}^m \beta_k I_k \left( 4 \ln 2 \frac{\rho d}{2\alpha^2} \right) e^{ik\varphi}, \end{aligned} \quad (5)$$

where  $I_k$  denotes the  $k$ -th modified Bessel function of the first kind (Roelofs et al. 2023). A stretched m-ring with ellipticity  $\tau$ , rotated by an ellipticity position angle  $\xi$  and width  $\alpha$  is given by  $\mathcal{I}(1 - \tau \cos(2(\varphi - \xi))\rho, \varphi; \alpha)$ .

We used a first-order (i.e.,  $m = 1$ ) stretched m-ring model as shown in Fig. 2, as it is the simplest case (e.g., Tiede et al. 2022a; Tiede & Broderick 2024). The ellipticity parameter  $\tau$  is defined as  $\tau = 1 - b/a$ , where  $a$  and  $b$  are the major and minor axes of the ellipse, respectively. The ellipticity position angle  $\xi$  represents the angle of the major axis  $a$ , measured counterclockwise from the north (east of north), as shown in Fig. 2. For this analysis, we kept the brightness position angle (PA),  $\eta$ , aligned with the ellipticity PA,  $\xi$ . Hence, we define  $\xi$  over the full range of 0 to 360°. We estimate the precision with which the parameters of this model, fit to data on April 21, 2018 at band 4, can be recovered. We employed the above Fisher information approach implemented within the ngEHTforecast package<sup>1</sup>. This method does not explicitly fit the m-ring model to the data. Instead, it performs a second-order expansion of the logarithmic probability density around the best-fit location, providing an estimate of the uncertainty of each of fitted parameter.

<sup>1</sup> <https://github.com/aeb/ngEHTforecast>, accessed with the git commit 115bf73.



**Fig. 2.** Definition of parameters  $\tau$ ,  $\xi$  for m-ring model, along with respective marginalized uncertainties using Fisher information analysis. Left: A visualization of a stretched m-ring model with parameters  $\tau = 0.1$ ,  $\xi = 45^\circ$ , a brightness asymmetry of 0.23, and a diameter of  $d = 46 \mu\text{as}$ , blurred with a Gaussian kernel with a full width at half maximum of  $10 \mu\text{as}$ . The brightness position angle,  $\eta = 45^\circ$ , is aligned with  $\xi$ . Right: Maps of marginalized uncertainties in the parameters  $\tau$  (top row) and  $\xi$  (bottom row) for m-ring models with various values of  $\tau$  and  $\xi$ , derived using Fisher information analysis on M87\* band 4 data.

The parameter precision estimates assume that the fitting process utilizes complex visibilities as input data, with broad priors imposed on the station gain amplitudes and phases for each scan (Pesce et al. 2022).

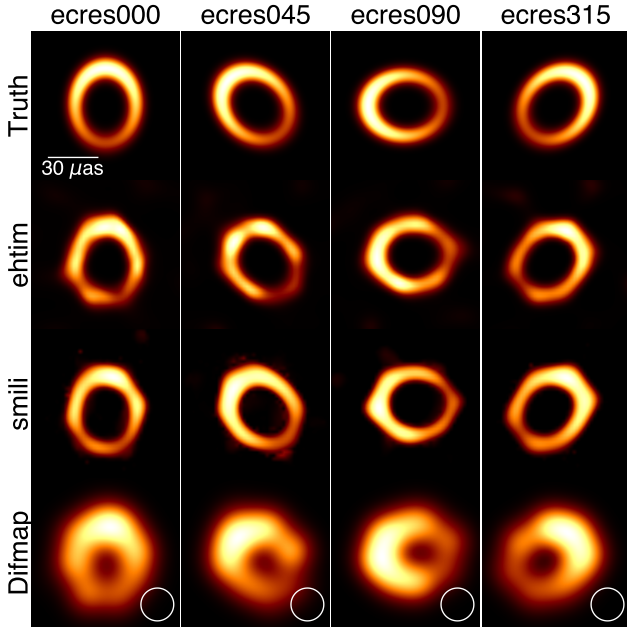
For this analysis, we tested m-ring models with  $\tau$  ranging from 0 to 0.3 and  $\xi$  ranging from 0 to  $360^\circ$ . The diameter of the thin elliptical m-rings is  $d = \sqrt{ab} = 46 \mu\text{as}$ , which is then blurred by a  $10 \mu\text{as}$  circular Gaussian (Tiede et al. 2022a). We assume a brightness asymmetry  $\beta_1 = 0.23$  for the m-ring (see Table 7 in M87\* 2018 I). Figure 2 shows the marginalized uncertainties  $\sigma_\tau$  and  $\sigma_\xi$ , calculated using Eq. (3), for the parameters  $\tau$  and  $\xi$ , respectively. We computed  $\sigma_\tau$  and  $\sigma_\xi$  for data with and without GLT to assess its relevance in  $(u, v)$ -coverage. As seen in Fig. 2,  $\sigma_\tau$  and  $\sigma_\xi$  are approximately three to five times larger for the data without GLT. This demonstrates that the additional  $(u, v)$ -coverage provided by GLT baselines enhances the precision in constraining  $\tau$  and  $\xi$ . Furthermore,  $\sigma_\tau$  and  $\sigma_\xi$  are nearly three times larger for the models with north-south alignment (i.e.,  $\xi = 0^\circ$  or  $180^\circ$ ). For models with the same  $\xi$  but different  $\tau$ ,  $\sigma_\tau$  and  $\sigma_\xi$  remain approximately constant. During the 2017 and 2018 EHT campaigns, the James Clerk Maxwell Telescope (JCMT) only recorded a single polarization feed, which could have contributed to systematic polarization leakage in 2018. To evaluate this issue, we performed a similar analysis for data without JCMT. As shown in Fig. 2, removing JCMT has a minimal effect ( $<10\%$ ) on the marginalized uncertainties of  $\tau$  and  $\xi$ . Therefore, JCMT data are retained for the remainder of the analysis.

### 3. Geometric tests

Before analyzing the M87\* data, two sets of tests with geometric models were conducted to evaluate the accuracy of the

imaging and feature extraction methods in recovering the true values and assessing potential biases in the imaging methods. We used geometric models with various ellipticity,  $\tau$ , and the position angle of the ellipse's major axis,  $\xi$  (north to east), to check potential biases depending on  $(u, v)$ -coverage. The first test selects the Top Set imaging parameter combinations of the RML and CLEAN methods using four elliptical crescent models ( $m = 1$ ) of  $\tau = 0.187$  and  $\xi = [0^\circ, 45^\circ, 90^\circ, 315^\circ]$ . The values of  $\tau$  and  $\xi$  are chosen to be consistent with Tiede et al. (2022a). The second test evaluates the ellipticity feature extraction using 42 elliptical crescent models ( $m = 1$ ) with  $\tau = [0.0, 0.05, 0.1, 0.15, 0.2, 0.25, 0.3]$  and  $\xi = [0^\circ, 60^\circ, 120^\circ, 180^\circ, 240^\circ, 300^\circ]$ . We used eht-imaging to generate synthetic data using the geometric models listed above. Before generating the synthetic data, we also added a milliarcsec-scale Gaussian to these geometric models. This Gaussian mimics jet emission on scales of milliarcseconds to arcseconds, to which short intra-site baselines of the EHT are sensitive (M87\* 2017 IV). We added station gain corruptions derived from M87\* and thermal noise to mimic the real observational data (M87\* 2018 I). Synthetic data with random gain corruptions are also tested using Bayesian imaging, where the posterior distribution of the gain parameters is estimated.

Imaging was performed using both forward and inverse modeling techniques. The forward modeling consists of RML and Bayesian methods, while the inverse modeling employs a CLEAN-based deconvolution method. For RML imaging, we used eht-imaging (Chael et al. 2016, 2018, 2019) and SMILI (Akiyama et al. 2017a,b, 2019). For Bayesian imaging, we used Comrade (Tiede 2022) and THEMIS (Broderick et al. 2020a,b). For CLEAN-based deconvolution, we used DIFMAP (Shepherd 1997, 2011). A more detailed explanation of each imaging method is provided in M87\* 2017 IV and M87\* 2018 I



**Fig. 3.** Elliptical crescent models with different ellipse position angles. From left to right, *ecres000*, *ecres045*, *ecres090*, and *ecres315*. From top to bottom, groundtruth images and fiducial images from *eht-imaging*, *SMILI*, and *DIFMAP* for band 4. *DIFMAP* images are presented with a beam convolution of a  $20\mu\text{as}$  circular Gaussian (M87\* 2018 I).

(see Appendix A for updates to the Bayesian imaging methods). We note that while M87\* 2018 I has employed both imaging methods and visibility domain model fitting, we focused on the imaging methods in this study.

### 3.1. Imaging parameter selection with the elliptical crescent models

The dataset for the first test is used to sub-select the Top Set imaging parameter combinations for the RML and CLEAN methods. Bayesian methods do not require a parameter survey, and thus the geometric models used in this step were not tested. Imaging results from the RML and CLEAN methods depend on a set of parameters determined by various imaging assumptions, including hyperparameters and optimization choices. Each combination of parameters can yield slightly different image morphology and fit quality for the data. Therefore, it is necessary to survey different parameter combinations and select those that provide the best fit to the data and most closely reproduce the groundtruth image (if from synthetic data), referred to as the Top Set. For *eht-imaging*, *SMILI*, and *DIFMAP*, the Top Set was previously selected in M87\* 2018 I based on four geometric models (*cres180*, *dblsrc*, *disk*, *ring*), using data from M87\*. The number of Top Set parameter combinations varies across methods due to differences in their parameter space. Additionally, variations between bands arise from different (systematic) uncertainties inherent to each dataset (see M87\* 2018 I). However, we did not test whether the Top Set parameters are valid for different elliptical structures. To investigate this, we selected a new Top Set by imaging four additional geometric models of elliptical crescents: *ecres000*, *ecres045*, *ecres090*, and *ecres315* (Fig. 3, top). The imaging survey is performed over the original Top Set from M87\* 2018 I, meaning the new Top Set corresponds to a subset of the original.

The Top Set selection is based on two metrics: (i) the normalized cross-correlation ( $\rho_{\text{NX}}$ ) between the reconstructed and

**Table 1.** Number of new Top Set parameter combinations.

Band	<i>eht-imaging</i>	<i>SMILI</i>	<i>DIFMAP</i>
Band 3	860/874 (98%)	4429/5333 (83%)	189/303 (62%)
Band 4	1332/1469 (91%)	3457/5108 (68%)	215/465 (46%)

**Notes.** This table shows the number of new Top Set parameter combinations compared to the original Top Set. The number ratio relative to the original Top Set is given in parentheses.

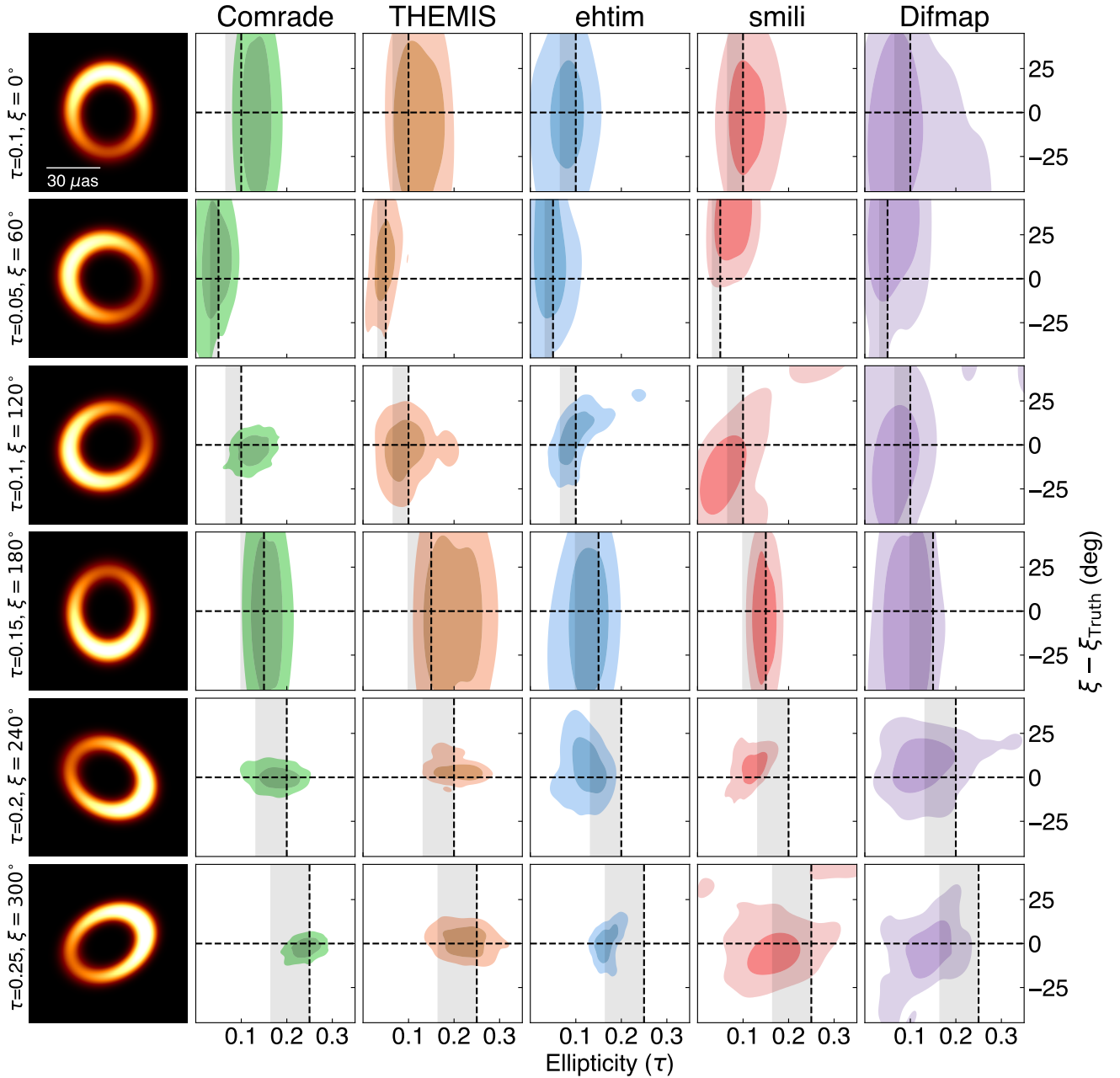
groundtruth images for synthetic data and (ii) the reduced  $\chi^2$  on the real M87\* data. Since the latter was already satisfied in the original Top Set (i.e.,  $\chi^2 < 2$ ), the new Top Set is selected solely on the  $\rho_{\text{NX}}$  of the elliptical crescent geometric models. The  $\rho_{\text{NX}}$  cutoff was determined in the same manner as described in M87\* 2017 IV and M87\* 2018 I, by convolving the groundtruth image with the effective resolution from the longest baseline ( $\sim 24\mu\text{as}$ ; see Fig. 1). Then, the cutoff value was determined as 0.75 for both band 3 and band 4, with no variations across the models.

As a result, several parameter combinations passed the thresholds, demonstrating their ability to reconstruct the elliptical crescent structure while distinguishing the structural position angle. Table 1 summarizes the number of new Top Set parameter combinations for each pipeline and band compared to the original Top Set. The images reconstructed using the fiducial parameters are shown in Fig. 3.

### 3.2. Evaluation with the elliptical crescent models

After selecting the new Top Set parameters for the RML (*eht-imaging* and *SMILI*) and CLEAN (*DIFMAP*) methods, we performed additional imaging of the geometric models using all methods for performance evaluation. The Bayesian methods, *THEMIS* and *Comrade*, do not require a Top Set selection since their only hyperparameters are the field of view and the number of pixels. Therefore, we directly performed the geometric tests with these two methods. For these models,  $\xi$  coincides with the position angle of the brightest spot (see Appendix B for tests with different alignments). This approach aims to identify specific cases where ellipticity or position angle models are not well recovered due to ( $u, v$ )-coverage limitations. To measure ellipticity and the ellipticity position angle, we used a stretched m-ring template from VIDA (Tiede et al. 2022b). For all feature extraction in this work, we used a m-ring of order four in azimuth and order one in width, following Tiede et al. (2022a).

Figure 4 presents a subset of the measured  $\tau - \xi$  distributions from the respective geometric model reconstructions for different imaging pipelines. The results indicate that  $\xi$  is less constrained at  $0^\circ$  and  $180^\circ$  due to relatively poorer ( $u, v$ ) coverage in these directions, as expected from the Fisher information analysis (Sect. 2). The measured ellipticity is still influenced by the underlying angular resolution. For instance, convolving the images and models with a  $5\mu\text{as}$  circular Gaussian reduces the ellipticity measurement of 0.1 by  $\sim 3\%$  (see Appendix C for more discussions about the resolution effect on measured ring features). In our results, the resolution limit of *DIFMAP* is given as  $\sim 20\mu\text{as}$  (M87\* 2018 I), while the forward modeling results from RML methods including Bayesian approaches can achieve super-resolution. Therefore, measured ellipticities from reconstructed images that are up to  $\sim 30\%$  lower than the true value are considered acceptable (gray shaded, vertical area in Fig. 4; see also Fig. C.1). As a result, all imaging methods successfully recovered the true  $\tau$  and  $\xi$  values within their own resolution limit. However, it is worth noting that, ignoring the resolution



**Fig. 4.** Subset ellipticity measurements for geometric models (6 out of 42) for all imaging methods. From left to right: groundtruth image of a given geometric model,  $\tau$ – $\xi$  distribution using Comrade, THEMIS, eht-imaging, SMILI, and DIFMAP for band 4 synthetic data. Each row corresponds to a different geometric model, with the true model shown in the leftmost column. The vertical and horizontal dashed lines in each panel of  $\tau$ – $\xi$  distribution indicate the true values. The contours denote 68% and 95% confidence intervals. The vertical dashed line shows  $\tau$  measured with VIDA for the groundtruth model. The gray shaded region spans the range of  $\tau$  values for the groundtruth model, from the unconvolved case to the convolution of a circular Gaussian of  $20 \mu\text{as}$  FWHM.

effects, the RML and deconvolution imaging methods tend to underestimate the ellipticity for models with extreme ellipticities in all 42 tests.

#### 4. Ring ellipticity of M87\* and its comparison with GRMHD simulation snapshots

##### 4.1. Ring ellipticity of M87\*

Following the geometric tests that validated the imaging pipelines and their parameter combinations for ellipticity mea-

surement, they were applied to the M87\* data<sup>2</sup> (see Fig. 5). The imaging results correspond to a subset of images in M87\* 2018 I for RML and CLEAN methods (Table 1), while remaining consistent for Bayesian methods. Ring features were extracted from the images using VIDA<sup>3</sup>, as summarized in Table 2. The measured ellipticities are consistent across all imaging approaches

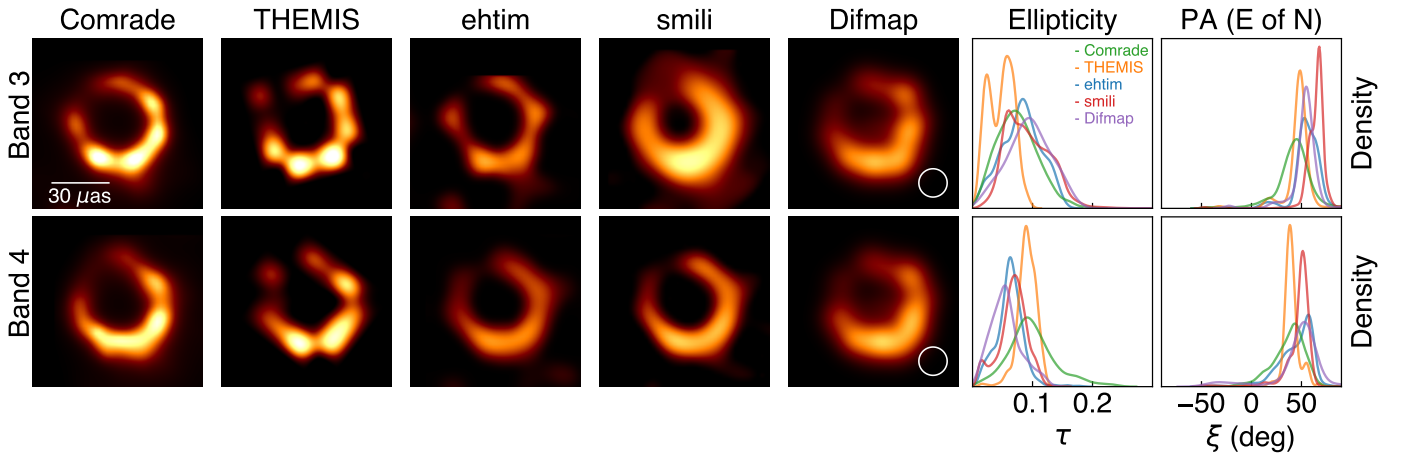
<sup>2</sup> Data accessed from [https://datacommons.cyverse.org/browse/iplant/home/shared/commons\\_repo/curated/EHTC\\_M87-2018\\_Mar2024/](https://datacommons.cyverse.org/browse/iplant/home/shared/commons_repo/curated/EHTC_M87-2018_Mar2024/)

<sup>3</sup> A m-ring model of first-order in width and fourth-order in azimuth template was used, consistent with the template used in the geometric tests (see also, Tiede et al. 2022a).

**Table 2.** Measured ellipticity and position angle for EHT 2018 M87\* images.

	Band	Comrade	THEMIS	eht-imaging	SMILI	DIFMAP	Average	Band average
$\tau$	Band 3	$0.07^{+0.04}_{-0.03}$	$0.05^{+0.02}_{-0.03}$	$0.07^{+0.03}_{-0.03}$	$0.09^{+0.04}_{-0.03}$	$0.10^{+0.04}_{-0.04}$	$0.07^{+0.03}_{-0.03}$	$0.08^{+0.03}_{-0.02}$
	Band 4	$0.09^{+0.04}_{-0.03}$	$0.09^{+0.01}_{-0.01}$	$0.06^{+0.02}_{-0.02}$	$0.07^{+0.02}_{-0.02}$	$0.05^{+0.03}_{-0.02}$	$0.08^{+0.03}_{-0.02}$	
$\xi$	Band 3	$44.1^{+10.5}_{-12.8}$	$48.3^{+4.0}_{-4.3}$	$56.0^{+9.8}_{-7.2}$	$66.6^{+2.3}_{-8.9}$	$54.2^{+6.2}_{-4.0}$	$53.5^{+6.0}_{-6.2}$	$50.1^{+6.2}_{-7.6}$
	Band 4	$40.0^{+11.2}_{-18.3}$	$38.9^{+6.0}_{-4.1}$	$48.4^{+10.6}_{-19.7}$	$50.4^{+4.9}_{-11.3}$	$52.4^{+6.5}_{-10.7}$	$44.0^{+6.7}_{-9.7}$	

**Notes.** Ellipticity,  $\tau$  (in rows labeled  $\tau$ ), and its position angle,  $\xi$  in degrees (in rows labeled  $\xi$ ), measured from the EHT 2018 M87\* images. The position angle  $\xi$  is measured east of north. For each method and band, the main value reported is the median, and the error range represents the  $1\sigma$  uncertainty around the median. The ‘‘Average’’ column provides the weighted median and  $1\sigma$  error across methods for each band. The ‘‘Band Average’’ column gives the overall weighted median and  $1\sigma$  error across all methods and both bands for  $\tau$  and  $\xi$ , respectively.



**Fig. 5.** EHT 2018 M87\* images and ellipticity ( $\tau$ ) and ellipticity position angle ( $\xi$ ) distributions. (left to right) Images from each imaging method (Comrade, THEMIS, eht-imaging, SMILI, and DIFMAP). For Comrade and THEMIS, mean posterior images are shown. Fiducial images from the respective Top Sets are shown for the other methods. The two right panels show the distributions of  $\tau$  and  $\xi$  for each method. Top and bottom rows show results for band 3 and band 4, respectively. Colors correspond to each method (see legend).

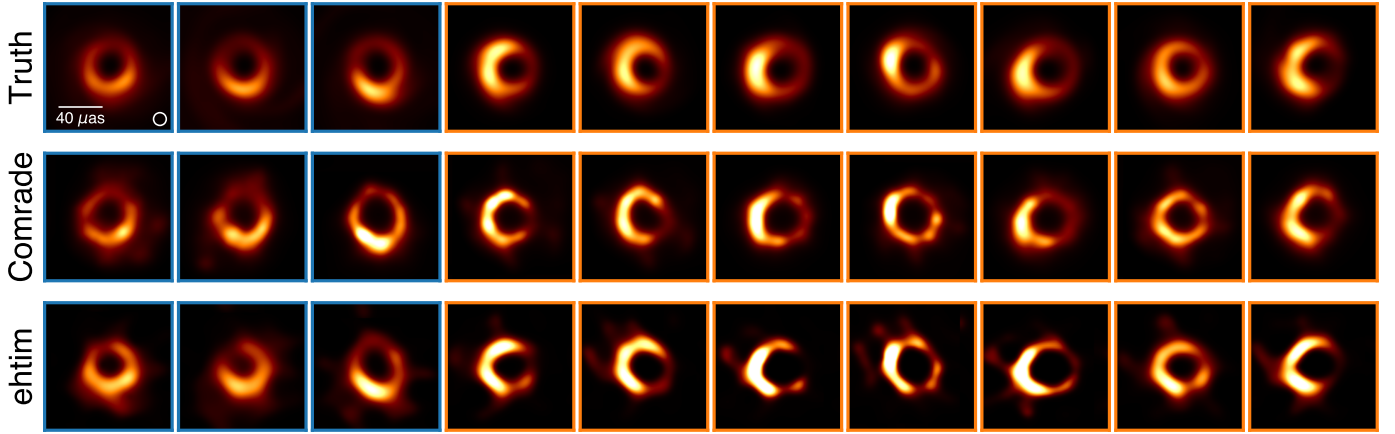
and at both frequency bands, 3 and 4, yielding an average ellipticity of  $\tau = 0.08^{+0.03}_{-0.02}$ . The average position angle of the ellipse is  $\xi = 50.1^{+6.2}_{-7.6}$  degrees, consistent across different imaging methods within  $2\sigma$ . The average across all methods and bands is computed by taking weighted median and  $1\sigma$  error. Given the relatively better performance of Bayesian imaging methods, as described in Sect. 3 and shown in Fig. 4, we computed the average  $\tau = 0.08^{+0.02}_{-0.02}$  and  $\xi = 44.4^{+5.8}_{-6.4}$  only from these methods. These averages are in good agreement with the values obtained by averaging over all methods. Notably, the direction of  $\xi$  is approximately aligned with the angle of brightest spot on the ring,  $\sim 200\text{--}230^\circ$  (M87\* 2018 I).

The measured  $\tau$  is also consistent with results of Tiede et al. (2022a), which reported  $\tau = 0\text{--}0.3$  and inferred accretion turbulence as the dominant source of the measured ellipticity, and with those of Tiede & Broderick (2024) which reported  $\tau = 0.09^{+0.07}_{-0.06}$ . We note that while this work used 2018 EHT observations, the above comparisons are made with the works that used 2017 EHT observations. The uncertainties in our results are lesser than those of previous studies from the 2017 EHT data, owing to the improved  $(u, v)$ -coverage in the 2018 EHT.

#### 4.2. Comparison with GRMHD simulations

With the results, we applied the same imaging and feature extraction methods to GRMHD models with different physi-

cal parameters to investigate the underlying physical dependencies. For this purpose, we used two GRMHD libraries of KHARMA (Prather et al. 2021) and BHAC (Porth et al. 2017). Thermal electron distribution (Maxwell-Jüttner distribution) models were drawn from KHARMA, while nonthermal electron distribution (kappa distribution) models were sourced from BHAC (Fromm et al. 2022; Cruz-Orsorio et al. 2022). Out of the 299 GRMHD models that were considered in M87\* 2018 II, we selected 218 models with an outflow power exceeding  $10^{42}$  erg/s (M87\* 2017 I, M87\* 2017 V, M87\* 2018 II). After the outflow threshold was applied, we selected 100 models for imaging and feature extraction, of which roughly 75% were thermal models and the remainder nonthermal. There were 18 models for each spin value of  $-0.94$ ,  $-0.5$ ,  $+0.5$ , and  $+0.94$  from the KHARMA thermal models, resulting in 72 thermal models in total. The remaining 28 models were chosen from the BHAC nonthermal models that met the threshold; we selected seven models for each spin. Since black hole spin and inclination determine a displacement of the inner shadow that can manifest as non-circularity (e.g., Tiede et al. 2022a), this sample can investigate the potential correlation between spin and ellipticity. Among the 100 selected GRMHD models, 83 are strongly magnetized, magnetically arrested disk (MAD) models, and 17 are weakly magnetized standard and normal evolution (SANE) models. Random snapshots were taken from each model and scaled to the best-fit mass based on snapshot scoring implemented in M87\* 2018 II.



**Fig. 6.** Subset of GRMHD images (10 out of 100 models) from KHARMA and BHAC libraries: (from top to bottom) ground truth, reconstructed images by Comrade (mean image) and eht-imaging (one random from Top Set) for band 4. Thermal models from KHARMA are marked in orange and nonthermal models are marked in blue. The ground truths are shown after blurring with a  $12\ \mu\text{as}$  circular Gaussian.

The scaling factor is a ratio of observed-to-simulated mass-to-distance ratios.

The scaled snapshots were then used to generate synthetic data following the same procedure described in Sect. 3. The synthetic data were imaged using eht-imaging and Comrade, as representatives of RML and Bayesian methods, respectively. As presented in Fig. 6, the images were consistent with the groundtruth. We then extracted the ellipticities from these images using VIDA and compared them with the true ellipticity. The groundtruth GRMHD snapshot images were convolved with a  $12\ \mu\text{as}$  circular Gaussian to take resolution effect into account. The  $12\ \mu\text{as}$  size corresponds to the obtained super-resolution from Comrade and eht-imaging, which is estimated by comparing  $\rho_{\text{NX}}$  of the original and blurred groundtruth images with different sizes of circular Gaussian kernel. This is an average from results for all 100 GRMHD models and is consistent between Comrade and eht-imaging. Figure 7 shows the differences of  $\tau$  and  $\xi$  between reconstructed images (from eht-imaging and Comrade) and the true values that are centered at zero in both parameters. This suggests that the observed ellipticity and its angle are real and not an artifact of the imaging process or instrumental limitations. The broader spread in  $\xi$  is due to models with low ellipticity, where the orientation angle is naturally more difficult to constrain.

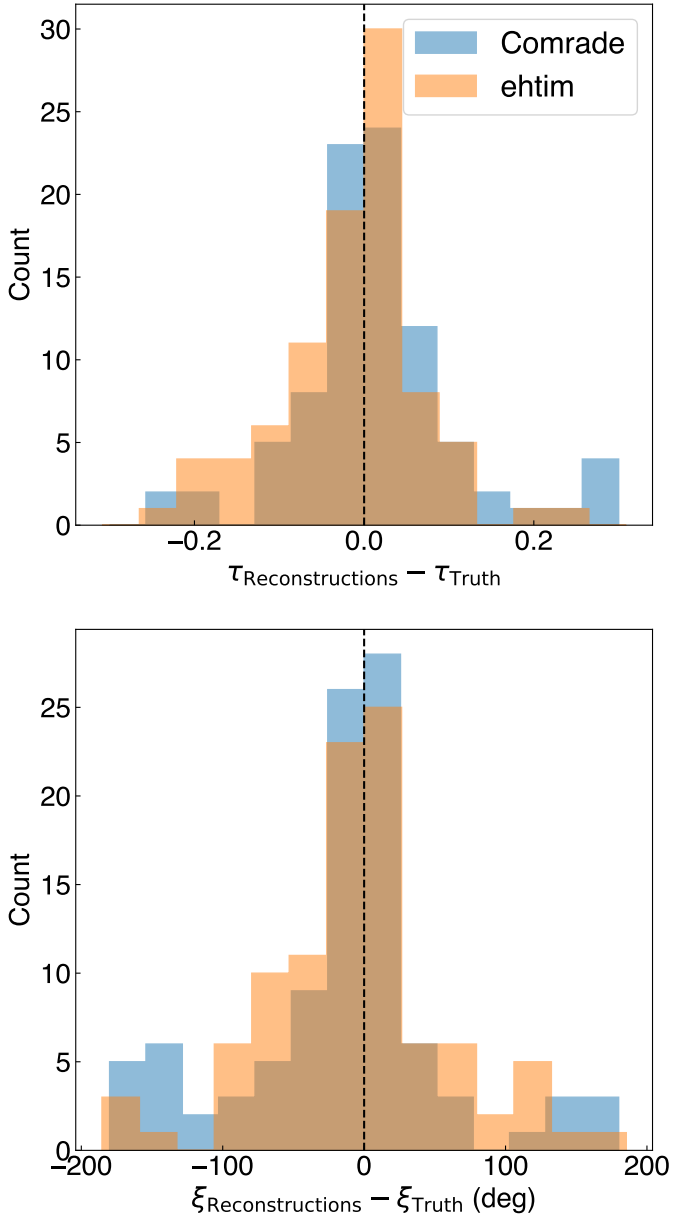
## 5. Origin of the M87\* ring ellipticity

As introduced in Sect. 1, observed ellipticity in EHT images can arise from two main sources: (i) gravitational ellipticity due to spacetime curvature and (ii) emission ellipticity from astrophysical structure. In this section, we focus on disentangling the contributions using GRMHD simulations with varying physical parameters. We utilized all 299 GRMHD models described in Sect. 4.2, which span a wide range of parameters, including black hole spin, electron distribution function (eDF) (thermal and nonthermal), magnetic field states (SANE and MAD), and ion-to-electron temperature ratios in both low- and high-density regions ( $R_{\text{low}}$  and  $R_{\text{high}}$ , respectively; see Mościbrodzka et al. 2016 for definitions). For each model, we measured the image ellipticity from the corresponding groundtruth GRMHD snapshot, scaled to the best-fit mass and blurred with a  $12\ \mu\text{as}$  Gaussian, as described in Sect. 4.2. Figure 8 shows that the

observed M87\* ellipticity is consistent with the distribution of all 299 GRMHD models, falling within their median and 68% confidence intervals.

General relativistic magnetohydrodynamic simulations are uniquely suited to probing both gravitational ellipticity and emission ellipticity. The gravitational ellipticity arises from the curvature of spacetime near the event horizon and is directly influenced by black hole spin. For instance, a Kerr black hole with spin of  $a = 0.94\text{--}0.999$  and viewed at an inclination of  $17^\circ$  can produce a gravitational ellipticity of  $\sim 0.02$  (see Fig. 8, top right). This level of distortion cannot explain the measured ellipticity of M87\*. Even if we consider a  $3^\circ$  uncertainty (Mertens et al. 2016) on the inclination of M87\*, with  $20^\circ$  inclination and spin  $a = 0.999$ , the maximum ellipticity reaches only  $\sim 0.03$  (Johnson et al. 2020). Moreover, as shown in Table 3 and Fig. 8, there is no statistically significant correlation between the spin and the measured ellipticity in full GRMHD images. This indicates that while spin contributes to the gravitational ellipticity, it does not dominate the total observed ellipticity in the images. Table 3 also shows no significant correlation between ellipticity and magnetic field state (SANE and MAD), implying that the global magnetic field structure does not have a strong influence on ellipticity. In contrast, Fig. 8 and Table 3 suggest that nonthermal models and simulations with higher values of  $R_{\text{high}}$  are correlated with larger emission ellipticity. Nonthermal models tend to generate more extended or diffuse emission, and increasing  $R_{\text{high}}$  shifts emission from the disk to the jet region; both effects increase the ellipticity of the ring in the image.

To quantify the role of asymmetric non-ring emission, we defined a “non-ring flux fraction” by subtracting the best-fit circular Gaussian ring (using VIDA) from each GRMHD image and setting negative residuals to zero. The ratio of the remaining positive flux to the total flux defines the non-ring flux fraction. We computed Spearman correlation coefficients between this quantity and the measured image ellipticity, using a bootstrapping method to account for sample variance (e.g., Curran 2014; Cheng et al. 2023). Figure 9 reveals a positive correlation between the non-ring flux fraction and ellipticity. We note that upon visual inspection, it does not seem that the outliers appear from transient flux eruption events. This supports the conclusion that emission ellipticity, driven by turbulent accretion structures outside the ring, is the dominant contributor to ellipticity in GRMHD images. These results suggest that the observed



**Fig. 7.** Histograms of differences in  $\tau$  (top) and  $\xi$  (bottom) between reconstructed and true GRMHD values. Results from Comrade (blue) and eht-imaging (orange) are shown, both centered around zero for each parameter.

ellipticity in the M87\* image is naturally explained by emission ellipticity arising from astrophysical effects such as turbulent accretion flow.

## 6. Summary and conclusions

In this study, we measured the ellipticity of the emission ring in the black hole images of M87\* using the EHT 2018 observations. Fisher information analysis was employed to first assess the feasibility of ellipticity measurements, after the addition of the GLT, which filled gaps in the north-south ( $u, v$ )-coverage. This analysis shows that the inclusion of the GLT improves the precision in constraining ellipticity parameters by  $\sim 3$ – $5$  times. With the improved ( $u, v$ )-coverage compared to the EHT 2017, we then managed to extract the ellipticity success-

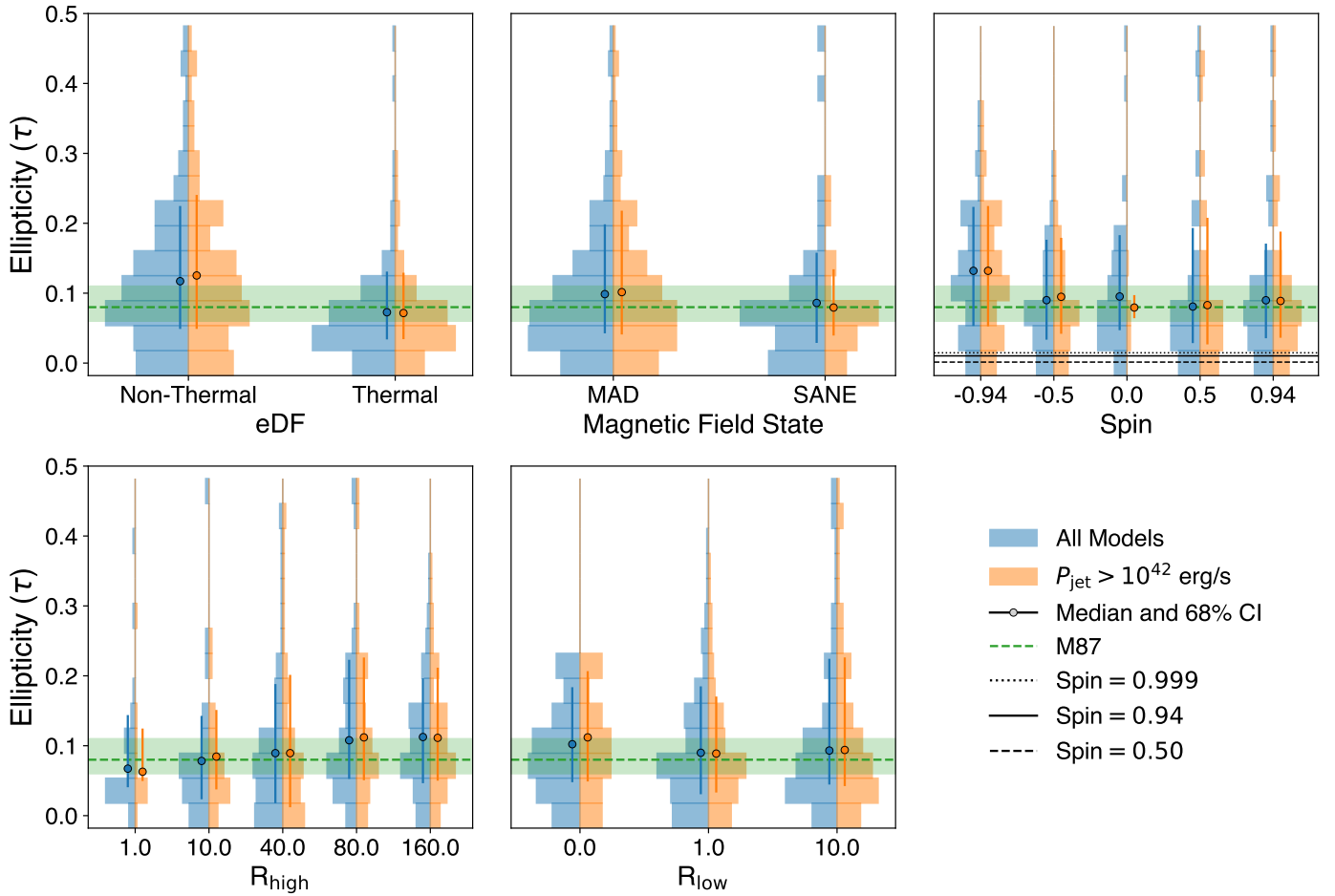
fully from five different methods that cross-compare the results. This is the first method-wide confirmation of the ellipticity measurement.

For imaging with the RML and deconvolution methods, the imaging parameter combinations were sub-selected from the original ones in M87\* 2018 I, based on imaging results for four elliptical geometric models. This step is not required for Bayesian imaging methods such as Comrade and THEMIS. All imaging methods (and parameters) were then evaluated using various geometric elliptical ring models with differing position angles and ellipticities, and they successfully recovered the groundtruth values in most cases.

Applying these approaches to the M87 data, we measured the ellipticity to be  $\tau = 0.08^{+0.03}_{-0.02}$  on average, with consistency across all imaging methods and previous findings from EHT 2017 (Tiede & Broderick 2024). In addition, the position angle of the ellipse is measured as  $\xi = 50.1^{+6.2}_{-7.6}$  degrees, indicating that the ring structure is slightly elongated along an axis that is roughly aligned with the brightest spot on the ring,  $\sim 200$ – $230^\circ$  (M87\* 2018 I). We also note that while Kim et al. (2025) reported  $\tau = 0.06 \pm 0.04$  for the image of M87 at 86 GHz, which is consistent with our measurements at 230 GHz, this is an astrophysical effect at 86 GHz. Comparison with GRMHD simulations first confirms that the measured ellipticity is real, but no strong constraints on the parameters including the spin are yet found. However, the parameters providing more non-ring flux (that is, nonthermal emission and higher  $R_{\text{high}}$ ) tend to reproduce larger ellipticity. This is confirmed by comparison with the non-ring flux fraction to the measured ellipticity. In line with this, to explain the measured ellipticity of M87, the astrophysical effects such as turbulent accretion flow are required. It is worth noting that the additional non-circularity by the inclined black hole (e.g., tilted accretion disk) or exotic spacetime are not completely ruled out.

With the current ground-based array, our ability to precisely measure the ellipticity of the emission ring is constrained by the dominance of turbulent astrophysical effects associated with the direct image (Gralla & Lupsasca 2020; Johnson et al. 2020). In the case of M87\*, detecting the gravitational influence on ellipticity, and hence measuring the spin, requires us to overcome these limitations through one of two approaches. The first approach involves continued long-term monitoring of M87\*, allowing for temporal averaging of the turbulent effects, thereby enabling the underlying gravitational signature to emerge more clearly. For instance, in Fig. 10, we present the measured ellipticities of 1000 snapshots spanning  $\sim 370$  days for one of the GRMHD models, along with the ellipticity of the time-averaged image in the right panel. The average image clearly reveals the photon ring, while the turbulent accretion flow is averaged out. This example illustrates that future observations could detect ellipticity arising from gravitational effects, as highlighted by the red line in the left panel.

The second approach entails space VLBI observations, which would provide the necessary angular resolution to detect the photon ring (Gralla et al. 2019; Johnson et al. 2020). Unlike the direct image, the photon ring is expected to be less affected by astrophysical turbulence, making it a more direct probe of the underlying spacetime structure and gravitational effects near the black hole. We also note that the direct image is more elliptical than the photon ring (see Figure 6 in Gralla & Lupsasca 2020). To better distinguish the relative effects on the



**Fig. 8.** Ellipticity of truth GRMHD models (blurred with  $12 \mu\text{as}$  Gaussian) for different GRMHD parameters. All 299 models are shown in blue, and the models that pass the jet power criteria are shown in orange (note that while plotting we combined the nonthermal models with the same parameters but different nonthermal emission fraction ( $\epsilon$ )). The over-plotting on the histograms shows the median value and the 68% confidence interval. The ellipticity of M87 is shown as a dashed green line, with its error range shown in the shaded green region. In the top rightmost panel, the ellipticity of the critical curve for a Kerr black hole (see Figure 7, Johnson et al. 2020) for different spins (inclination =  $17^\circ$ ) is plotted to compare it with the histograms of the respective spins. The spin = 0.5 case is shown by dashed black line; the spin = +0.94 is represented by a solid black line and the spin = +0.999 case is given by a dotted black line.

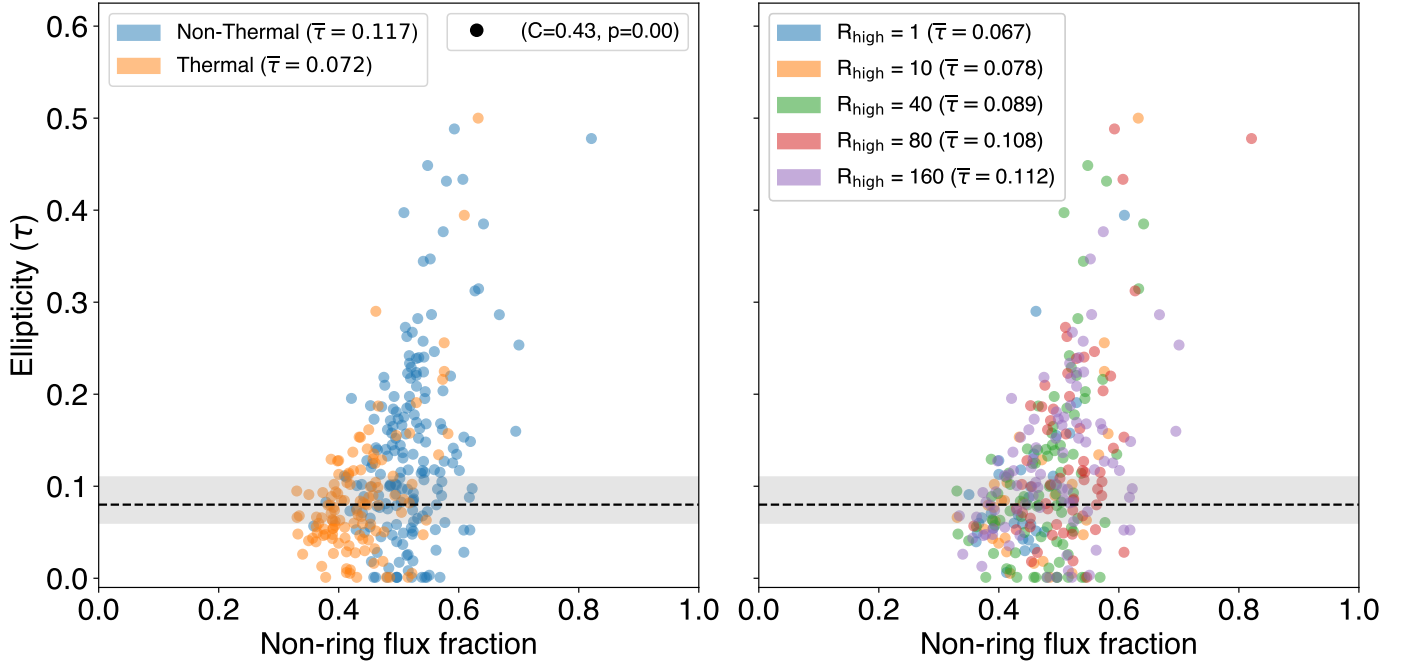
**Table 3.** Spearman correlation for ellipticity of GRMHD truth models and their physical parameters.

Models	eDF	Magnetic field state	Spin	$R_{\text{high}}$	$R_{\text{low}}$
All	$C = -0.31, p = 0.05$	$C = -0.09, p = 0.44$	$C = -0.12, p = 0.22$	$C = 0.20, p = 0.04$	$C = -0.02, p = 0.50$
$P_{\text{jet}} > P_0$	$C = -0.35, p = 0.03$	$C = -0.17, p = 0.26$	$C = -0.13, p = 0.18$	$C = 0.22, p = 0.03$	$C = -0.02, p = 0.48$

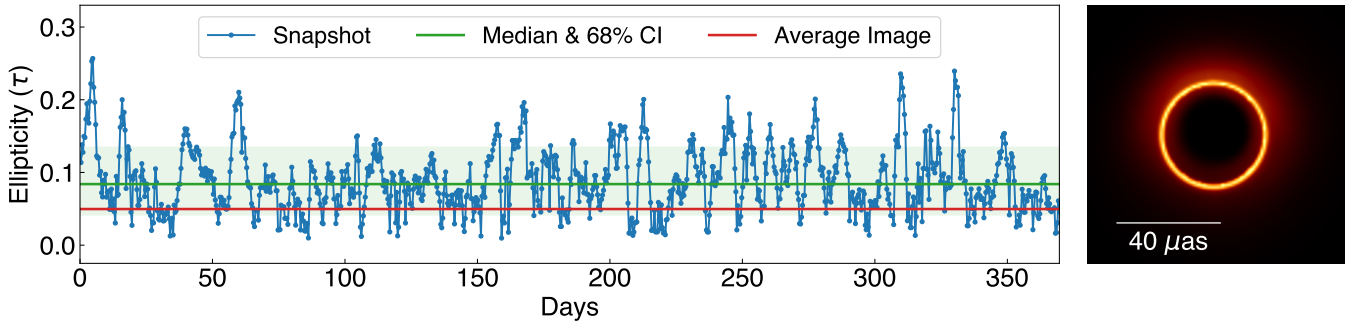
**Notes.** Spearman correlation coefficient  $C$  and its associated  $p$ -value for the ellipticity of GRMHD truth models and their physical parameters. These were computed using a bootstrapping method (e.g., Curran 2014; Cheng et al. 2023). A  $p$ -value  $\leq 0.05$  indicates a rejection of the null hypothesis that the parameters are not correlated. Cases considered correlated ( $p \leq 0.05$ ) are highlighted in green.  $P_0 = 10^{42}$  erg/s is the jet-power threshold applied to the models.

ellipticity from different potential origins, higher precision measurements of ellipticities from better angular resolution are necessary. Looking ahead, future observations with higher angular resolution, such as those from the next-generation EHT (ngEHT; Johnson et al. 2023; Doeleman et al. 2023), the Event Horizon Imager (EHI; Roelofs et al. 2019), the Terahertz Exploration and Zooming-in for Astrophysics (THEZA;

Gurvits et al. 2022), and the Black Hole Explorer (BHEX; Johnson et al. 2024; Akiyama et al. 2024), will offer further constraints by resolving finer photon ring structures. As demonstrated by the addition of the GLT to the EHT array, the inclusion of future sites in the EHT and ngEHT arrays will improve the precision of measurements of the ring ellipticity of M87\*.



**Fig. 9.** Ellipticity of all 299 GRMHD truths (convolved with  $12\ \mu\text{s}$  Gaussian) compared with the non-ring flux fraction. The left and right panels are the same, but the colors are different for (non)thermal models (left) and  $R_{\text{high}}$  values (right). The ellipticity of M87 is shown by a dashed black line, with its error range shown in the shaded gray region. The median  $\tau$  for each case is shown in the legend.



**Fig. 10.** Ellipticities of 1000 snapshots spanning  $\sim 370$  days for a GRMHD model with the following parameters: magnetic field configuration = MAD; thermal eDF; black hole spin =  $-0.5$ ;  $R_{\text{high}} = 160$ ,  $R_{\text{low}} = 1$ ; and inclination angle =  $17^\circ$ . The ellipticity of each snapshot is measured after blurring with a  $12\ \mu\text{s}$  Gaussian (blue). The median and 68% confidence interval of the time series are shown with a solid green line and shaded region, respectively. The ellipticity of the time-averaged image (right) is shown with a red line.

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## Appendix A: Bayesian imaging methods

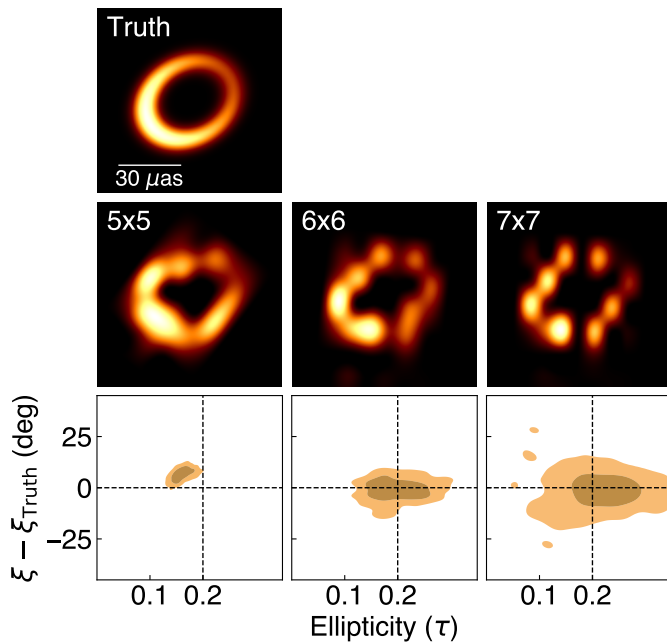
In [M87\\* 2018 I](#), THEMIS used a  $5 \times 5$  pixel grid (raster) as it was used in [M87\\* 2017 IV](#). Since this size, may not be suitable for the 2018 EHT coverage or elliptical rings, similar to [Tiede & Broderick \(2024\)](#), we performed a small survey of different imaging models, changing the number of pixels and computing the Bayesian evidence to find the optimal raster size. The Bayesian evidence ( $Z$ ) of a model  $M$  with parameters  $\theta$  is given by,

$$Z(M) = \int \mathcal{L}(\mathcal{V}|\theta, M)p(\theta, M)d\theta. \quad (\text{A.1})$$

where  $\mathcal{L}$  is the log-likelihood, and  $\mathcal{V}$  is the observed data. In a Bayesian setting, the optimal model corresponds to the one with the highest evidence. The Bayesian evidence was computed using thermodynamic integration ([Lartillot & Philippe 2006](#)), utilizing the parallel tempering scheme from [Syed et al. \(2021\)](#). Given the computational complexity of running a survey for each set of data, we instead focused on one of the geometric elliptical ring synthetic datasets in Sect. 3. Specifically, we considered the elliptical ring with  $\tau = 0.1$  and  $\xi = 120^\circ$ . The evidence for this survey is given in Tab A.1. According to these values,  $6 \times 6$  raster has the highest evidence. Furthermore, Fig. A.1, which shows how the true value of  $\tau = 0.1$  and  $\xi = 120^\circ$  is recovered correctly by the  $6 \times 6$  raster. Hence, throughout the analysis in this paper, we used the  $6 \times 6$  raster for THEMIS.

**Table A.1.** Evidence of different raster sizes.

Raster size	$5 \times 5$	$6 \times 6$	$7 \times 7$
Evidence	-2890	-2885	-2889



**Fig. A.1.** Evaluation of different rasters of THEMIS through synthetic data tests. The true m-ring model with  $\tau=0.1$  and  $\xi = 120^\circ$  is shown on the top. The posterior mean images from THEMIS for  $5 \times 5$ ,  $6 \times 6$ , and  $7 \times 7$  rasters are shown in the middle.  $\tau$  and  $\xi - \xi_{\text{Truth}}$  posteriors are shown at the bottom. The contours are shown for 68% and 95% confidence intervals. The dashed line marks the truth values.

In [M87\\* 2018 I](#), Comrade imaging used closure phases and visibility amplitudes as the data products, and fit only for gain amplitudes. The prior used for the raster assumed that the pixels are independently distributed (Dirichlet prior). There have been several developments in Comrade since then. In this paper, we used complex visibilities as the data products and fit for both amplitude and phase gains (with reference to one station). The image model is a  $64 \times 64$  raster with a field of view of  $200 \mu\text{as}$ . An extended Gaussian component was used to model the emission on milliarcsecond scales. The location, position angle, and fractional flux are the model parameters, while the size is fixed as  $1000 \mu\text{as}$ . The total flux of the image plus the Gaussian component was fixed to  $1.1 \text{ Jy}$  as assumed in network calibration for the [M87\\*](#) data. For the raster, we use a first-order Gaussian Markov random field (GMRF) prior on the log-ratio transformed pixel intensities. Hence, the pixels are spatially correlated. The GMRF is added to a mean image which is a  $40 \mu\text{as}$  Gaussian (size of the Gaussian does not drastically change the reconstructed images). The variance and correlation length of the random field are the hyperparameters. The variance and the correlation length are included as parameters in the model. The amplitude gain priors are the same as used in [M87\\* 2018 I](#). We allow gains to vary every scan. For the gain phases, the gain phase for ALMA is set to be zero. In the case when ALMA is not present in the scan, we select the next reference station alphabetically. For rest of the gain phase priors, we use von Mises prior with zero mean and a concentration parameter  $\pi^{-2}$  (which is essentially a uniform prior on the interval  $[-\pi, \pi]$ ). Sampling is performed using [Hoffman & Gelman \(2014\)](#), in the Julia sampling package `AdvancedHMC.jl`<sup>4</sup>, in the same way as done in [M87\\* 2018 I](#).

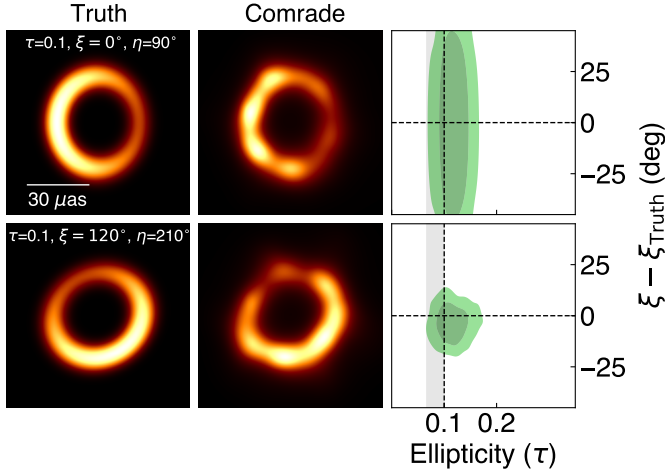
## Appendix B: Additional geometric tests

In Sect. 3, we performed the tests with geometric models where the ellipticity position angle  $\xi$  was aligned with the brightness position angle  $\eta$ . In order to be certain that an offset between position angles, will not introduce any additional biases in measuring ellipticity, we performed this additional test shown in Fig. B.1. We chose the  $\eta$  to be perpendicular to  $\xi$  to test the extreme case. This test was performed with Comrade for all  $\tau$  and  $\xi$  but Fig. B.1 shows only the two cases when  $\xi = 0^\circ$  and  $\xi = 120^\circ$ . In all cases, Comrade recovers the true  $\tau$  correctly. For  $\xi$ , we see the same pattern as seen in Fig. 4 and as mentioned in Sect. 3. Even in these tests, we found that true  $\xi$  can be recovered with narrow posteriors for all cases, except when  $\xi$  is aligned North-South, for which we get broad posteriors.

## Appendix C: The effect of resolution on the measured ellipticity

VIDA stretched m-ring template models the ellipticity of a m-ring by stretching a symmetric m-ring template in  $x$ -direction and compressing it in  $y$ -direction. Assuming this definition of measured ellipticity, we want to solve for an analytical equation that relates  $\tau$  with a Gaussian blurring kernel. To do so, consider a zero-order symmetric m-ring with flux  $F_0$  and radius  $r_0$ ,  $\frac{F_0}{2\pi r_0} \delta(r - r_0)$ , which has a Fourier transform given by,  $F_0 J_0(2\pi r_0 |u|)$ .  $J_0$  is a zeroth-order Bessel function of the first kind and  $u, v$  are the spatial coordinates in the Fourier domain. Stretching the m-ring in the  $u$ -direction by  $\beta$  and compressing in the  $v$ -direction by  $\beta$ ,

<sup>4</sup> <https://github.com/TuringLang/AdvancedHMC.jl>



**Fig. B.1.** Geometric tests for the cases when brightness PA  $\eta$  is perpendicular to  $\xi$ . The leftmost column shows the ground truth for the cases  $\tau = 0.1$ ,  $\xi = 0^\circ$ ,  $\eta = 90^\circ$  (top) and  $\xi = 120^\circ$  (bottom). Mean images from Comrade posteriors are shown in the middle. The rightmost column shows measured  $\tau$  and  $\xi$  posteriors (68% and 95% confidence contours) compared with true values in dashed lines. The gray shaded region marks the region between  $\tau$  of the groundtruth model without any convolution and with convolution of a Gaussian up to  $20 \mu\text{as}$  size.

we get:

$$\tilde{I}(u, v; r_0, \tau) = F_0 J_0 \left( 2\pi r_0 \sqrt{\frac{u^2}{1-\tau} + (1-\tau)v^2} \right) \quad (\text{C.1})$$

where  $\tilde{I}(u, v)$  is the intensity profile in the Fourier domain (or the amplitude visibilities at  $u, v$ ),  $\tau = 1 - b/a = 1 - (2r_0\beta)/(2r_0/\beta) = 1 - \beta^2$ . If we blur this stretched m-ring with a circular Gaussian of full-width at half maximum (FWHM)  $\alpha$ , we get,

$$\tilde{I}(u, v; r_0, \tau, \alpha) = \tilde{I}(u, v; r_0, \tau) \times \exp\left(\frac{-\pi^2 |u|^2 \alpha^2}{4 \log 2}\right) \quad (\text{C.2})$$

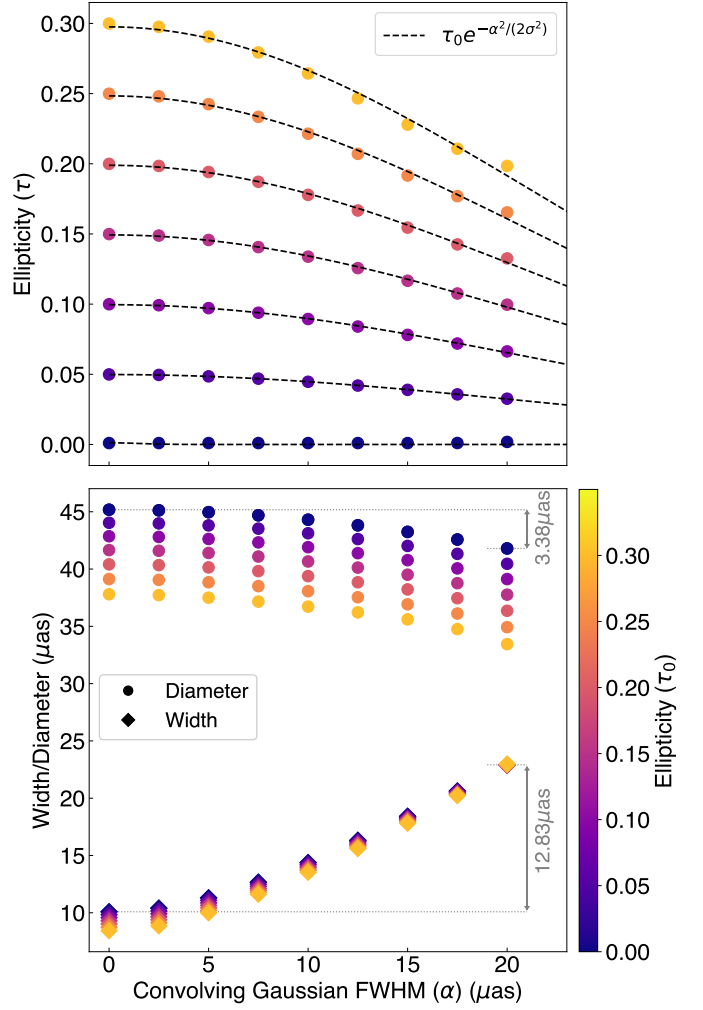
From Eq. C.2, it is not possible to get a  $\tau - \alpha$  relation without the  $u$  and  $v$  dependence. Instead, we used geometric elliptical m-ring models with  $\xi = 120^\circ$  and  $\tau_0 = [0.05, 0.1, 0.15, 0.2, 0.25, 0.3]$  and measured the ellipticity with VIDA by blurring the models with different circular Gaussian FWHM ( $\alpha$ ). We then fitted a Gaussian to each measured  $\tau - \alpha$  data (see Eq. C.3) for all different  $\tau_0 - \xi$  models.

$$\tau = A * e^{-(\alpha-\mu)^2/(2\sigma^2)} \quad (\text{C.3})$$

When Eq. C.3 is fit to different  $\tau - \alpha$  data for the  $\tau_0$  cases, we get  $\mu = 0$  and  $A = \tau_0$  for all the cases as shown in Eq. C.4.

$$\tau = \tau_0 e^{-\alpha^2/(2\sigma^2)} \quad (\text{C.4})$$

where  $\sigma$  was measured as  $21.5 \pm 0.5 \mu\text{as}$  for all the cases. We note that we have data only up to one  $\sigma$  of the fitted Gaussians. The drop in  $\tau$  is high when  $\tau_0$  is high, as shown in Fig. C.1 (top). The maximum change is seen in the  $\tau_0 = 0.3$  case, when it is blurred by  $\alpha = 20 \mu\text{as}$ ,  $\tau$  goes from 0.3 to  $\sim 0.225$ . When  $0.05 < \tau_0 < 1.0$ , given the nominal resolution of  $\sim 20 \mu\text{as}$ , the change in true ellipticity  $\Delta\tau$  is  $0.017 \lesssim \Delta\tau \lesssim 0.034$ . While the diameter of the m-ring drops by a maximum of  $\sim 4 \mu\text{as}$ , the width increases by a maximum of  $\sim 13 \mu\text{as}$ , after blurring with  $\alpha = 20 \mu\text{as}$  as shown in Fig. C.1 (bottom).



**Fig. C.1.** The effect of blurring with different Gaussian FWHM ( $\alpha$ ) on the ring parameters measured by VIDA. (Top) Ellipticity of a stretched m-ring with true  $\xi = 120^\circ$  and  $\tau_0 = [0.05, 0.1, 0.15, 0.2, 0.25, 0.3]$ . The black dashed line marks the fitted curves. (Bottom) Diameter (circle) and width (diamond) of a stretched m-ring with the same true  $\xi$  and  $\tau_0$  as on the top.

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