Price spikes in the electricity markets: how and why

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ABSTRACT

Since their liberalization, the electricity markets are characterized by a rather high volatility, which includes

price spikes as one of the stylized and specific characteristics of this market. In this paper, we investigate the

factors and mechanisms determining these spikes. Based on the Italian electricity market data, we perform a

specific analysis of the auctions mechanisms and of the hourly bid and offer of electricity characteristics, for

determining how and why do price spikes occur.

Keywords: Electricity markets; auctions; bid and offer; price spikes; probit model.

JEL Classification: Q41, D43

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1. Introduction

As a consequence of the liberalization of electricity markets, in the largest part of western countries the electricity power market is based on a day-ahead auction mechanism, where, for each hour, each producer and each distributor can place its offer, and the price is subsequently determined as the one that allows the electricity power bid and offer to be balanced. This auction mechanism, due to the variability of the electricity demand, determines a continuous variation in the resulting prices. Thus, the electricity prices time series have often been analyzed by statistical models similar to the ones developed for financial markets, as like stock exchange or similar. Indeed, some characteristics are specific of electricity markets. Among these, one of the stylized facts that characterize the electricity prices time series is the presence of price spikes, not necessarily related to corresponding variations in its demand quantity. Almost all the models in literature include this characteristic, which is well known in its effects, but not adequately analyzed in its mechanisms and determinants.

In this paper, we analyze in detail the Italian electricity market, in its day-ahead auction mechanism, including the single producers behavior, and the aggregate bid and offer resulting curves. In this way, we can evidence the specific mechanisms that determine significant variations in prices, not due to demand variations.

We firstly investigate thoroughly the explanatory variables, which can affect spike prices by means of probit regression techniques. We highlight that high demand only explains part the actual price spikes. Thus, the second step of the analysis is devoted to investigate in depth the auction mechanisms, taking into account the characteristics of the bid and ask curves coming from the auctions and of the single producers behavior, so to find how and why do spikes occur.

The reminder of this paper is structured as follows. Section 2 reports the literature review; Section 3 investigates about the main features of the electricity markets, the auction mechanisms and the price spikes in the Italian Market. Section 4 concludes.

2. LITERATURE REVIEW

Price spikes are one of the stylized facts that characterize energy markets, and have been investigated from a theoretical point of view by several authors. Indeed, a large part of the literature is focused on spikes description and forecasting. The most significant and recent contributions concerning electricity price modeling and the occurring of price spikes can be summarized as it follows.

Christensen et al. (2012) interpret the time series of price spikes as a discrete-time point process and they forecast spikes for the Australian Market. Clements et al. (2015) additionally investigate price spikes across connected regions also in the Australian Market. Handika et al. (2014) survey the influence of exogenous variables (such as load, weather, capacity constraints) on the occurrence and intensity of price spikes in Australian Market. At this purpose, they apply the Heckman selection model. Huisman (2008) asserts that the occurrence of spikes increases whenever temperature deviates from its mean levels. Janczura et al. (2013) investigate about spikes estimation through filtering techniques. Manner et al. (2016) treat simultaneous occurrence of spikes in several markets by applying an innovative dynamic model. Mount et al. (2006) use a stochastic regime-switching model to determine spikes. This model is indeed suitable to characterize the volatile nature of electricity prices. Ullrich (2012) uses high frequency spot price data coming from several markets in order to estimate volatility and consequently the occurrence of price spikes.

Finally, A review of electricity price modeling is contained in Weron (2014).

3. POWER MARKETS

3.1 MAIN CHARACTERISTICS OF POWER MARKETS

The electricity markets are currently coping with important transformations with the introduction of the category of renewable energies. Since the years around 2000, the European Union went on a comprehensive energy market deregulation, aiming to a multinational energy market able to integrate renewable energy sources. The EU directive on the promotion of renewable energy sources, entered into effect in June 2009,

setting national targets in the aim of reaching a minimum of 20% renewable energy sources (RES) share by 2020.

A striking peculiarity of electricity markets is that electricity production and consumption must be in equilibrium at any time, to prevent network collapses.

The main part of the power spot market is managed by means of a day-ahead market, where each producer (distributor) proposes its offer for the supply (demand) for each hour of the next day, specifying the requested price and the power quantity. The auction mechanism identifies the price which equilibrates demand and supply of power, and assigns the production slots to each producer which has offered a price lower or equal to the equilibrium price.

In Italy, the auction is administered by GME ("Gestore Mercati Energetici") which is a state managed company. Within this market, due to the particular structure of the Italian power grid, the auctions can be managed by regional zones, and the final price paid by customers refers to the so-called "single national purchase price" PUN ("Prezzo Unico Nazionale"), estimated for each hour through a weighted average of the zonal prices issued by the day-ahead market, where each zone weight depends on the actually traded quantities.

3.2 THE AUCTIONS MECHANISM

The day-ahead electricity power auction market can be considered as a Cournot oligopoly of N power producers, each one able to choose the production level, and the minimum price they are accepting, but not the actual price they will receive, which is determined as the auction clearing price. For a survey of Cournot oligopoly in power markets, see Vespucci et al. (2010).

In general, a Cournot oligopoly with N agents can be represented as it follows:

- a fixed number N > 1 of agents, all producing the same homogeneous good, known to all agents;
- the agents do not cooperate, and each agent's output decision affects the good's price;
- agents compete in quantities and price. Each one chooses it simultaneously to the other agents; in particular, each i firm chooses quantity q_i and price p_i ;
- the market-clearing price p^* of the good is determined by a commonly known function, which

allows the good demand and offer to be balanced;

- all the agents offering their production at a price lower or equal to the clearing price are allowed to
 sell the offered quantity at the clearing price, while the producers offering at a price higher than the
 clearing price p* will have their offer not accepted;
- the agents are economically rational and act strategically, seeking to maximize their profit; agent i has a marginal cost function $c_i(q_i)$, and its total profit u_i is given by $u_i = q_i \cdot p * -c_i(q_i)$.

Figure 1 provides a graphical description of the auction mechanism.

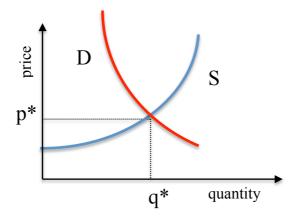


Fig. 1 Day ahead auction graphical representation

3.3 PRICES SPIKES IN THE ITALIAN POWER MARKET

Price spikes are defined as the prices exceeding a preset threshold.

In literature, some different approaches are proposed. Some authors suggest to use log-price change thresholds, fixed (as in Bierbrauer and Weron, 2004) or variable (Cartea et al. (2005).

Other authors suggest using a fixed threshold value for the whole time series under consideration (e.g. Amjady and Keynia, 2010; Christensen, 2012; Clements 2015). As our sample includes the daily values from 2012 to 2016, so including different market conditions, not correctly selected by a fixed threshold, similarly to (Lu et al. 2005, Voronin and Partanen, 2013) we computed the spike threshold as the price average plus three times its volatility recorded during the previous year.

More formally, we denote P_t the electricity price at time t (time unit is expressed in hours). We say that a price spike occurs whenever $P_t > \mu_t + 3\sigma_t$ where μ_t represents the mean price value and σ_t denotes its

volatility. Both quantities have been estimated by considering a rolling window of one-year data before time *t*. This definition allows classifying about *1%* of price values as spikes.

3.4 DEMAND-DRIVEN SPIKES

A statistical investigation highlights that spikes do not occur uniformly through time, indeed they are likely to cluster around particular periods. In this purpose, we analyzed the Italian electricity market behavior from 2005 to 2016. In the following figures, we picture the percentage of price spikes with respect to Year (Figure 2a), Month (Figure 2b), Day of the week (Figure 2c) and Hour (Figure 2d).

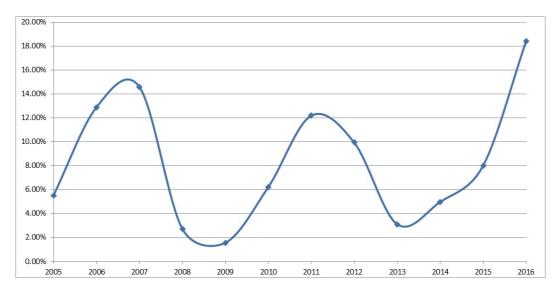


Fig. 2a: Price spikes incidence per Year

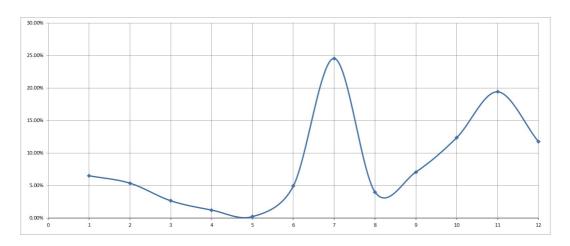


Fig. 2b: Price spikes incidence per Month ('1' = Jan, and so on)

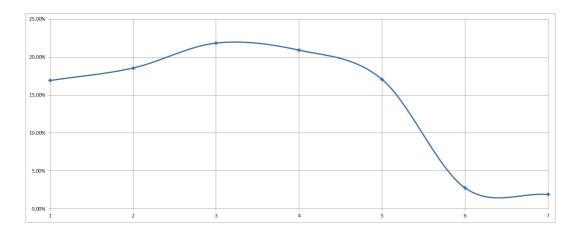


Fig. 2c: Price spikes incidence per Day of the week ('1' = Monday, and so on)

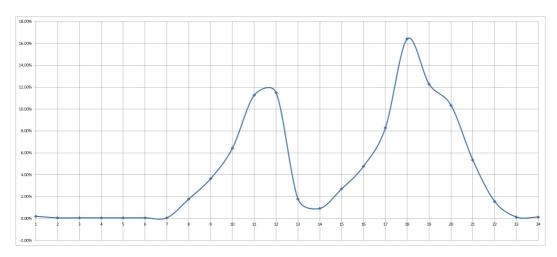


Fig. 2d: Price spikes incidence per Hour

The evidences coming from the previous figures can be interpreted as due to the higher electricity power demand. In fact, price spikes more often occur around July and November as cooling and heating starts. With reference to the week days, the price spikes occurrence is almost constant in working days, but its incidence is drastically reduced on Saturdays and Sundays. Regarding the hours of typical occurrence, the spikes attain two maxima at around 11-12 a.m. and 6 p.m., which approximately coincides with the timing of higher electricity demand. Finally, we note that spikes occurrence is not homogeneous through years.

For a more precise quantification of the actual role of demand in inducing price spikes, we performed some probit regression, taking into account data from 2012 to 2016, for a total of 43,848 records.

The first regression only includes demand as explanatory variable, in its direct value and nonlinear transformations (squared and cubed value), and lagged values (2 and 5 hours). Results show that only small

part of the spikes occurrence is explained by the demand volume, the resulting R-squared value being around 24% (see model 1 in appendix for details).

As the time span considered for our analysis includes important variations of production costs, we also verified if the introduction of some variables related to fuel costs could actually improve the estimation quality.

Thus, we also considered the effect of fuel prices such as crude oil and natural gas, which are one of the main determinants of the direct costs of fuel-based productions, and are expected to affect the resulting price for a given demand volume. Results show that these variables improve the estimation, raising the R-squared value to around 33% (see model 2 in appendix for details).

These results proof that the demand variations are not sufficient to explain the price spikes probability to occur, but an important part of its occurrence is still unexplained.

3.5 NON-DEMAND-DRIVEN SPIKES

For evaluating which mechanism can induce these results, we analyzed in depth the auction mechanism and bid and offer curves characteristics for determining how and why these "unexplained" price spikes do occur.

Price elasticity

The price elasticity (of supply or of demand) is a measure used in economics to quantify the responsiveness of the quantity supplied (or demanded) of a good or service to a change in its price.

The elasticity is defined as the percentage change in the quantity supplied divided by the percentage change in its price. Namely:

$$e_p = \frac{\Delta Q / Q}{\Delta p / p} = \frac{\Delta Q}{\Delta p} \cdot \frac{p}{Q}$$

Where e_p is the price elasticity, Q is the good (or service) quantity, ΔQ its variation, p the good (or service) price and Δp its variation.

In terms of its absolute value, an elasticity coefficient lower than one is typically read as an inelastic response to price changes, while a value greater than one signals an elastic response to price changes. With reference to the value sign, supply elasticity is typically positive, while demand is typically negative.

Figure 3 reports a typical auction session, with its demand and offer curves, and the resulting closing price and quantity.

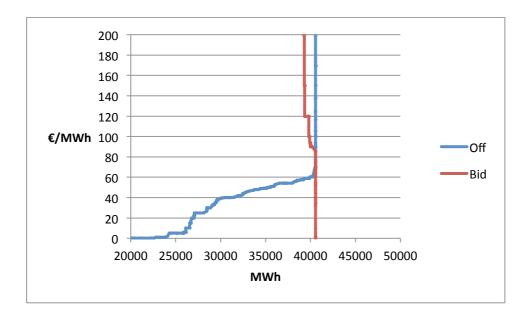


Fig. 3: Actual Italian electric market bid/off curves

Demand curve characteristics

It is important to analyze the actual bid and offer curves characteristics. The first evidence in Figure 3 is that the demand (bid) curve is highly inelastic, and that the main part of the demanded quantity is at "no price", so the buyers are willing to accept all resulting prices for the main part of the requested power. This means that the effect of prices variations is only slightly affecting the demanded quantity of electricity.

• Offer curve characteristics

The offer curve shows a completely different ongoing, which can be split into three main parts with different characteristics.

The first part (up to 23,000 MWh in Figure 3) is flat, and refers to offers at zero price, so it is due to producers willing to sell their production at whatever price the auction will determine (highly elastic). The second part (23,000 to 40,000 MWh in Figure 3) part is gradually rising, with a variable but limited slope (elastic). The third part (from around 40,000 MWh on in Figure 3) is almost vertical (inelastic).

One base reference coming from microeconomics is that, for a producer, it is worth selling the product as soon as its price is higher than its variable costs. In this way, all the variable costs needed for producing the

output are covered, and if the price is higher than this threshold, the difference can also cover the fixed costs, and, after the coverage of fixed costs, produce some income.

The three parts of the offer curve reflect the technology differences among the producers. The first part is typically due to RES, characterized by almost no variable costs, so that any positive price gives a positive contribution to the producer revenue, thus, it is worth selling all the production at whatever price.

The second part is typically related to fuel based productions, characterized by a significant cost for each MWh of power production, which is different for different fuels and technologies. In this case, it is worth selling the production only when the fuel and, more in general, marginal costs are covered by the resulting price. As the different technologies (and different power plants) are characterized by different marginal costs (see Table 2), the resulting curve reflects these differences, and each time the price goes up, some more plant can be accepted for covering the electricity demand. This results in variable slopes for the curve.

Power Plant technology	Guaranteed Cold Start-Up Time [h]	Marginal Costs [€/MWh]
Wind turbine	∞	1
Hydroelectric power station	0.02	1
Gas turbine	0.12	90
Cogeneration plant (CHP)	0.17	50
Combined cycle gas turbine	5	50
Hard coal power plant	6	60
Lignite power plant	9	40
Nuclear power plant	50	5

Data from Grimm, V. (2007) (start-up times) and Butler, L. and Neuhoff, K. (2008) (marginal costs).

Table 2 start-up times and marginal costs for some technologies

The final part of the curve is due to possible but limited overproductions of some power plant, with high variable costs.

Renewable sources impact

From the previous description, it is evident that the effect of any variability of RES offered quantity impacts on the first part of the offer curve. This happens quite often, as within the RES productions we typically have significant variations, e.g. due to the solar light daily variation, to the wind variations and to the river flows

variations. These production variations impact on the zero price offers, continuously changing in a significant way its total volume.

Instead, the fuel-based productions have no significant variations within the day, so the second part of the curve is characterized by a relative stability.

As described above, the auction mechanism is based on the producers offers, ordered on the offered price.

Thus, a reduction in the offered quantity at zero price, actually shifts the supply curve, denoted by S in figure 4, to the left, e.g. as in the new curve S'.

This horizontal shifting actually affects the auction results: as evident in figure 4, the clearing quantity falls from q^* to q^{**} while the clearing price rises from p^* to p^{**} .

Both demand and supply elasticity are fundamental, as a high elasticity determines small variations in the clearing price and quantity. Instead, rigidity increases the effect of variations to the clearing values. In particular when both curves are rigid, as when the demand volume is high, thus crossing the offer curve in its right side, near to the maximum production capability, even small variations can cause important jumps in the resulting price.

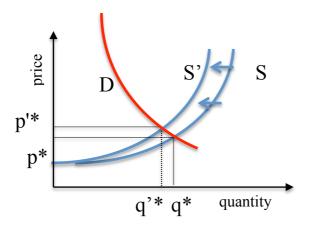


Fig. 4 Effect of the RES production reduction on the auction clearing quantity and price

An example of this effect is highlighted in the following Figure 5, reporting the offer curve shift from 7 p.m. to 8 p.m. of the same day (11/09/2015), causing a price variation from 84.27 to 92.17 €/MWh even if the demand, in the same hour, has had some reduction.

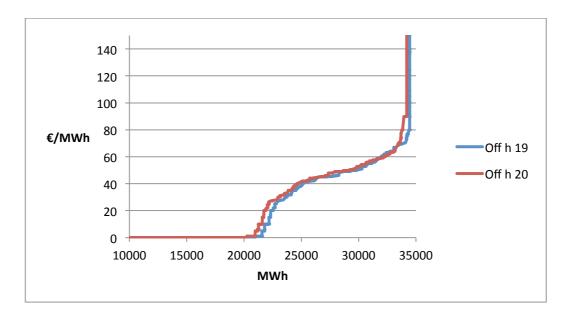


Fig. 5: Example of supply shifting in the Italian day-ahead electricity market

With reference to the Italian electricity market, Figure 6 reports the share of each of the main production technologies for year 2014, signaling an effective impact of RES.

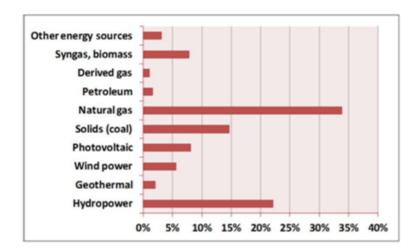


Fig. 6 Electricity production sources for year 2014 – Italy (Terna annual report)

For the reasons reported above, the changes in the zero offers (RES production), shifts to the left the offer curve, and, due to the rigidity of the demand curve, this results in significant variations in the auction closing price. But when the demanded production is near to the third (almost vertical) part of the offer curve, even small reductions in the zero offers can induce price spikes.

4. CONCLUSIONS

The electricity markets are extremely volatile and the electricity prices often exhibit abrupt spikes. This is one of the striking peculiarities of these markets. In order to face this price risk, futures and power derivatives have been settled by financial industry. The main goal of our paper is to explain the complex mechanisms that provoke price spikes, not adequately addressed in literature. Analyzing the Italian market, we showed that demand peaks only explain a small part of price spikes.

Thus, we have examined in detail the auction mechanism that characterizes the day-ahead electricity market.

Results show that the rigidity that characterizes both the demand curve and part of the supply curve is the fundamental determinant of price spikes.

More specifically, when demand values are high, both curves are characterized by a high rigidity, and even small variations of the demanded quantity or of the offered production have a high impact on the resulting clearing prices.

In this process, the variations of RES production turned out to be fundamental. In fact, even if at a first glance the RES production volume seems not impacting, as it is typically offered at zero price, in fact, it shifts the whole supply curve, and its effect results to be highly impacting.

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Appendix

Model 1: Probit, using 43,843 observations

Variable	Coefficient	Std. error	Z	p-value	significance
const	-55.0557	8.88217	-6.198	5.70e-10	***
demand	0.00407	0.00068	6.006	1.90e-09	***
demand _lag2	-6.83276e-05	7.03114e-06	-9.718	2.53e-22	***
demand lag5	2.48008e-05	4.19369e-06	5.914	3.34e-09	***
demand ^2	-1.03906e-07	1.70983e-08	-6.077	1.22e-09	***
demand ^3	9.09128e-13	1.42697e-13	6.371	1.88e-10	***

^{***} signals parameter significance at 1%, ** significance at 5% and * significance at 10%.

McFadden R-squared 0.2409

Adjusted R-squared 0.2390

Model 2: Probit, using 43,314 observations

Variable	Coefficient	Std. error	Z	p-value	significance
const	-76.83500	9.938140	-7.731	1.06e-014	***
demand	0.005528	0.000759	7.276	3.43e-013	***
demand _lag2	-7.99335e-05	7.86542e-06	-10.16	2.91e-024	***
demand _lag5	3.20417e-05	4.69250e-06	6.828	8.59e-012	***
demand ^2	-1.43841e-07	1.92410e-08	-7.476	7.68e-014	***
demand ^3	1.27359e-012	1.61226e-013	7.899	2.80e-015	***
oil_price	-0.25669	0.036439	-7.044	1.86e-012	***
oil_price_lag168	0.53456	0.057385	9.315	1.22e-020	***
oil_price_lag366	-0.24342	0.024738	-9.840	7.59e-023	***
gas_price	-4.08770	0.645664	-6.331	2.44e-010	***
gas_price_lag168	5.92652	0.683609	8.669	4.34e-018	***
oil*gas_price	0.02302	0.007680	2.998	0.0027	***
oil*gas_price_lag168	-0.040030	0.007928	-5.049	4.44e-07	***

McFadden R-squared 0.3350

Adjusted R-squared 0.3307

Historical time series for oil (Europe Brent Spot Price FOB - Dollars per Barrel) and gas (Henry Hub Natural Gas Spot Price - Dollars per Million Btu) come from on the U.S. Energy Information Administration (http://www.eia.gov).

The Oil and gas variables included in the regression, are obtained on the base of daily values, and computed as the average price of the previous 30 days, on a rolling window.